

# Package: latentFactorR (via r-universe)

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**Title** Data Simulation Based on Latent Factors

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**Description** Generates data based on latent factor models. Data can be continuous, polytomous, dichotomous, or mixed. Skews, cross-loadings, wording effects, population errors, and local dependencies can be added. All parameters can be manipulated. Data categorization is based on Garrido, Abad, and Ponsoda (2011) <doi:10.1177/0013164410389489>.

**Depends** R (>= 3.6.0)

**License** GPL (>= 3.0)

**Imports** BBmisc, EGAnet, fspe, googledrive, ineq, lavaan, Matrix, methods, mlr, mvtnorm, psych, rstudioapi, xgboost

**Suggests** ggplot2

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**Repository** <https://alexchristensen.r-universe.dev>

**RemoteUrl** <https://github.com/alexchristensen/latentfactor>

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latentFactorR-package    *latentFactorR-package*

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## Description

Generates data based on latent factor models. Data can be continuous, polytomous, dichotomous, or mixed. Skew, cross-loadings, and population error can be added. All parameters can be manipulated. Data categorization is based on Garrido, Abad, and Ponsoda (2011).

## Author(s)

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## References

- Christensen, A. P., Garrido, L. E., & Golino, H. (2022). Unique variable analysis: A network psychometrics method to detect local dependence. *PsyArXiv*
- Garrido, L. E., Abad, F. J., & Ponsoda, V. (2011). Performance of Velicer's minimum average partial factor retention method with categorical variables. *Educational and Psychological Measurement, 71*(3), 551-570.
- Golino, H., Shi, D., Christensen, A. P., Garrido, L. E., Nieto, M. D., Sadana, R., ... & Martinez-Molina, A. (2020). Investigating the performance of exploratory graph analysis and traditional techniques to identify the number of latent factors: A simulation and tutorial. *Psychological Methods, 25*(3), 292-320.

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add\_cross\_loadings      *Adds (Substantial) Cross-loadings to [simulate\\_factors](#) Data*

---

### Description

Intended to add substantial cross-loadings to simulated data from [simulate\\_factors](#). See examples to get started

### Usage

```
add_cross_loadings(
  lf_object,
  proportion_cross_loadings,
  proportion_cross_loadings_range = NULL,
  magnitude_cross_loadings,
  magnitude_cross_loadings_range = NULL,
  leave_cross_loadings = FALSE
)
```

### Arguments

**lf\_object**      Data object from [simulate\\_factors](#)

**proportion\_cross\_loadings**  
 Numeric (length = 1 or factors). Proportion of variables that should be cross-loaded randomly onto one other factor. Accepts number of variables to cross-load onto one other factor as well

**proportion\_cross\_loadings\_range**  
 Numeric (length = 2). Range of proportion of variables that should be cross-loaded randomly onto one other factor. Accepts number of variables to cross-load onto one other factor as well

**magnitude\_cross\_loadings**  
 Numeric (length = 1, factors, or total number of variables to cross-load across all factors). The magnitude or size of the cross-loadings. Must range between -1 and 1.

**magnitude\_cross\_loadings\_range**  
 Numeric (length = 2). The range of the magnitude or size of the cross-loadings. Defaults to NULL

**leave\_cross\_loadings**  
 Boolean. Should cross-loadings be kept? Defaults to FALSE. Convergence problems can arise if cross-loadings are kept, so setting them to zero is the default. Only set to TRUE with careful consideration of the structure. Make sure to perform additional checks that the data are adequate

### Value

Returns a list containing the same parameters as the original `lf_object` but with updated data, `population_correlation`, and parameters (specifically, loadings matrix). Also returns original `lf_object` in `original_results`

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**References**

Christensen, A. P., Garrido, L. E., & Golino, H. (2022). Unique variable analysis: A network psychometrics method to detect local dependence. *PsyArXiv*

**Examples**

```
# Generate factor data
two_factor <- simulate_factors(
  factors = 2, # factors = 2
  variables = 6, # variables per factor = 6
  loadings = 0.55, # loadings between = 0.45 to 0.65
  cross_loadings = 0.05, # cross-loadings N(0, 0.05)
  correlations = 0.30, # correlation between factors = 0.30
  sample_size = 1000 # number of cases = 1000
)

# Add substantial cross-loadings
two_factor_CL <- add_cross_loadings(
  lf_object = two_factor,
  proportion_cross_loadings = 0.25,
  magnitude_cross_loadings = 0.35
)

# Randomly vary proportions
two_factor_CL <- add_cross_loadings(
  lf_object = two_factor,
  proportion_cross_loadings_range = c(0, 0.25),
  magnitude_cross_loadings = 0.35
)

# Randomly vary magnitudes
two_factor_CL <- add_cross_loadings(
  lf_object = two_factor,
  proportion_cross_loadings = 0.25,
  magnitude_cross_loadings_range = c(0.35, 0.45)
)

# Set number of cross-loadings per factor (rather than proportion)
two_factor_CL <- add_cross_loadings(
  lf_object = two_factor,
  proportion_cross_loadings = 2,
  magnitude_cross_loadings = 0.35
)
```

---

add\_local\_dependence *Adds Local Dependence to [simulate\\_factors](#) Data*

---

### Description

Adds local dependence to simulated data from [simulate\\_factors](#). See examples to get started

### Usage

```
add_local_dependence(
  lf_object,
  method = c("correlate_residuals", "minor_factors", "threshold_shifts"),
  proportion_LD,
  proportion_LD_range = NULL,
  add_residuals = NULL,
  add_residuals_range = NULL,
  allow_multiple = FALSE
)
```

### Arguments

lf_object	Data object from <a href="#">simulate_factors</a>
method	Character (length = 1). Method to generate local dependence between variables. Only "correlate_residuals" at the moment. Future developments will include minor factor and threshold-shift methods. Description of methods: <ul style="list-style-type: none"> <li>• "correlate_residuals" — Adds residuals directly to the population correlation matrix prior to data generation (uses population correlation matrix from <a href="#">simulate_factors</a>)</li> <li>• "minor_factors" — Coming soon...</li> <li>• "threshold_shifts" — Coming soon...</li> </ul>
proportion_LD	Numeric (length = 1 or factors). Proportion of variables that should be locally dependent across all or each factor. Accepts number of locally dependent values as well
proportion_LD_range	Numeric (length = 2). Range of proportion of variables that are randomly selected from a random uniform distribution. Accepts number of locally dependent values as well. Defaults to NULL
add_residuals	Numeric (length = 1, factors, or total number of locally dependent variables). Amount of residual to add to the population correlation matrix between two variables. Only used when method = "correlated_residuals". Magnitudes are drawn from a random uniform distribution using +/- 0.05 of value input. Can also be specified directly (same length as total number of locally dependent variables). General effect sizes range from small (0.20), moderate (0.30), to large (0.40)

add\_residuals\_range Numeric (length = 2). Range of the residuals to add to the correlation matrix are randomly selected from a random uniform distribution. Defaults to NULL

allow\_multiple Boolean. Whether a variable should be allowed to be locally dependent with more than one other variable. Defaults to FALSE. Set to TRUE for more complex locally dependence patterns

### Value

Returns a list containing:

data Simulated data from the specified factor model

population\_correlation Population correlation matrix with local dependence added

original\_correlation Original population correlation matrix *before* local dependence was added

correlated\_residuals A data frame with the first two columns specifying the variables that are locally dependent and the third column specifying the magnitude of the added residual for each locally dependent pair

original\_results Original lf\_object input into function

### Author(s)

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### References

Christensen, A. P., Garrido, L. E., & Golino, H. (2023). Unique variable analysis: A network psychometrics method to detect local dependence. *Multivariate Behavioral Research*, 1–18.

### Examples

```
# Generate factor data
two_factor <- simulate_factors(
  factors = 2, # factors = 2
  variables = 6, # variables per factor = 6
  loadings = 0.55, # loadings between = 0.45 to 0.65
  cross_loadings = 0.05, # cross-loadings N(0, 0.05)
  correlations = 0.30, # correlation between factors = 0.30
  sample_size = 1000 # number of cases = 1000
)

# Add local dependence
two_factor_LD <- add_local_dependence(
  lf_object = two_factor,
  proportion_LD = 0.25,
  add_residuals = 0.20,
```

```
    allow_multiple = FALSE
  )

  # Randomly vary proportions
  two_factor_LD <- add_local_dependence(
    lf_object = two_factor,
    proportion_LD_range = c(0.10, 0.50),
    add_residuals = 0.20,
    allow_multiple = FALSE
  )

  # Randomly vary residuals
  two_factor_LD <- add_local_dependence(
    lf_object = two_factor,
    proportion_LD = 0.25,
    add_residuals_range = c(0.20, 0.40),
    allow_multiple = FALSE
  )

  # Randomly vary proportions, residuals, and allow multiple
  two_factor_LD <- add_local_dependence(
    lf_object = two_factor,
    proportion_LD_range = c(0.10, 0.50),
    add_residuals_range = c(0.20, 0.40),
    allow_multiple = TRUE
  )
)
```

---

add\_method\_factors      *Adds Methods Factors to [simulate\\_factors](#) Data*

---

## Description

Adds methods factors to simulated data from [simulate\\_factors](#). See examples to get started

## Usage

```
add_method_factors(
  lf_object,
  proportion_negative = 0.5,
  proportion_negative_range = NULL,
  methods_factors,
  methods_loadings,
  methods_loadings_range = 0,
  methods_correlations,
  methods_correlations_range = NULL
)
```

**Arguments**

lf_object	Data object from <code>simulate_factors</code> . Data <b>must</b> be categorical. If data are not categorical, then there function with throw an error
proportion_negative	Numeric (length = 1 or factors). Proportion of variables that should have negative (or flipped) dominant loadings across all or each factor. Accepts number of variables as well. The first variables on each factor, up to the corresponding proportion, will be flipped. Set to 0 to not have any loadings flipped. Defaults to 0.50
proportion_negative_range	Numeric (length = 2). Range of proportion of variables that are randomly selected from a uniform distribution. Accepts number of number of variables as well. Defaults to NULL
methods_factors	Numeric
methods_loadings	Numeric
methods_loadings_range	Numeric
methods_correlations	Numeric
methods_correlations_range	Numeric

**Value**

Returns a list containing:

data	Biased data simulated data from the specified factor model
unbiased_data	The corresponding unbiased data prior to replacing values to generate the (biased) data
parameters	Bias-adjusted parameters of the lf_object input into function
original_results	Original lf_object input into function

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**References**

Garcia-Pardina, A., Abad, F. J., Christensen, A. P., Golino, H., & Garrido, L. E. (2024). Dimensionality assessment in the presence of wording effects: A network psychometric and factorial approach. *Behavior Research Methods*.



**Examples**

```

# Generate factor data
two_factor <- simulate_factors(
  factors = 2, # factors = 2
  variables = 6, # variables per factor = 6
  loadings = 0.55, # loadings between = 0.45 to 0.65
  cross_loadings = 0.05, # cross-loadings N(0, 0.05)
  correlations = 0.30, # correlation between factors = 0.30
  sample_size = 1000, # number of cases = 1000
  variable_categories = 5 # 5-point Likert scale
)

# Add methods factors
two_factor_methods_effect <- add_method_factors(
  lf_object = two_factor,
  proportion_negative = 0.50,
  methods_loadings = 0.20,
  methods_loadings_range = 0.10
)

```

---

add\_population\_error    Adds Population Error to [simulate\\_factors](#) Data

---

**Description**

Adds population error to simulated data from [simulate\\_factors](#). See examples to get started

**Usage**

```

add_population_error(
  lf_object,
  cfa_method = c("minres", "ml"),
  fit = c("cfi", "rmsea", "rmsr", "raw"),
  misfit = c("close", "acceptable"),
  error_method = c("cudeck", "yuan"),
  tolerance = 0.01,
  convergence_iterations = 10,
  leave_cross_loadings = FALSE
)

```

**Arguments**

lf_object	Data object from <a href="#">simulate_factors</a>
cfa_method	Character (length = 1). Method to generate population error. Defaults to "ml". Available options: <ul style="list-style-type: none"> <li>• "minres" — Minimum residual</li> </ul>

	<ul style="list-style-type: none"> <li>• "ml" — Maximum likelihood</li> </ul>
fit	Character (length = 1). Fit index to control population error. Defaults to "rmsr". Available options: <ul style="list-style-type: none"> <li>• "cfi" — Comparative fit index</li> <li>• "rmsea" — Root mean square error of approximation</li> <li>• "rmsr" — Root mean square residuals</li> <li>• "raw" — Direct application of error</li> </ul>
misfit	Character or numeric (length = 1). Magnitude of error to add. Defaults to "close". Available options: <ul style="list-style-type: none"> <li>• "close" — Slight deviations from original population correlation matrix</li> <li>• "acceptable" — Moderate deviations from original population correlation matrix</li> </ul> <p>While numbers can be used, they are <b>not</b> recommended. They can be used to specify misfit but the level of misfit will vary depending on the factor structure</p>
error_method	Character (length = 1). Method to control population error. Defaults to "cudeck". Description of methods: <ul style="list-style-type: none"> <li>• "cudeck" — Description coming soon... see Cudeck &amp; Browne, 1992 for more details</li> <li>• "yuan" — Description coming soon...</li> </ul>
tolerance	Numeric (length = 1). Tolerance of SRMR difference between population error correlation matrix and the original population correlation matrix. Ensures that appropriate population error was added. Similarly, verifies that the MAE of the loadings are not greater than the specified amount, ensuring proper convergence. Defaults to 0.01
convergence_iterations	Numeric (length = 1). Number of iterations to reach parameter convergence within the specified 'tolerance'. Defaults to 10
leave_cross_loadings	Boolean. Should cross-loadings be kept? Defaults to FALSE. Convergence problems can arise if cross-loadings are kept, so setting them to zero is the default. Only set to TRUE with careful consideration of the structure. Make sure to perform additional checks that the data are adequate

## Value

Returns a list containing:

data	Simulated data from the specified factor model
population_correlation	Population correlation matrix with local dependence added
population_error	A list containing the parameters used to generate population error: <ul style="list-style-type: none"> <li>• error_correlation — Correlation matrix with population error added (same as population_correlation)</li> </ul>

- fit — Fit measure used to control population error
- delta — Minimum of the objective function corresponding to the misfit value
- misfit — Specified misfit value
- loadings — Estimated CFA loadings after error has been added

original\_results

Original lf\_object input into function

### Author(s)

[bifactor](#) authors

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### References

Cudeck, R., & Browne, M.W. (1992). Constructing a covariance matrix that yields a specified minimizer and a specified minimum discrepancy function value. *Psychometrika*, 57, 357–369.

### Examples

```
# Generate factor data
two_factor <- simulate_factors(
  factors = 2, # factors = 2
  variables = 6, # variables per factor = 6
  loadings = 0.55, # loadings between = 0.45 to 0.65
  cross_loadings = 0.05, # cross-loadings N(0, 0.05)
  correlations = 0.30, # correlation between factors = 0.30
  sample_size = 1000 # number of cases = 1000
)

# Add small population error using Cudeck method
two_factor_Cudeck <- add_population_error(
  lf_object = two_factor,
  cfa_method = "minres",
  fit = "rmsr", misfit = "close",
  error_method = "cudeck"
)

# Add small population error using Yuan method
two_factor_Yuan <- add_population_error(
  lf_object = two_factor,
  cfa_method = "minres",
  fit = "rmsr", misfit = "close",
  error_method = "yuan"
)
```

---

add\_wording\_effects    *Adds Wording Effects to [simulate\\_factors](#) Data*

---

### Description

Adds wording effects to simulated data from [simulate\\_factors](#). See examples to get started

### Usage

```
add_wording_effects(
  lf_object,
  method = c("acquiescence", "difficulty", "random_careless", "straight_line", "mixed"),
  proportion_negative = 0.5,
  proportion_negative_range = NULL,
  proportion_biased_cases = 0.1,
  proportion_biased_variables = 1,
  proportion_biased_variables_range = NULL,
  proportion_biased_person = 1,
  proportion_biased_person_range = NULL
)
```

### Arguments

lf_object	Data object from <a href="#">simulate_factors</a> . Data <b>must</b> be categorical. If data are not categorical, then there function with throw an error
method	Character (length = 1). Method to generate wording effect to add to the data. Description of methods: <ul style="list-style-type: none"> <li>• "acquiescence" —Generates new data with flipped dominant loadings (based on proportion_negative) and ensures a bias such that variables have a restricted range of responding (e.g., only 4s and 5s on a 5-point Likert scale)</li> <li>• "difficulty" —Generates new data with flipped dominant loadings (based on proportion_negative) and uses this data as the data without wording effects. Then, the signs of the dominant loadings are obtained and the dominant loadings are made to be absolute. Finally, the skews are multiplied by the signs of the original dominant loadings when generating the data with the wording effects</li> <li>• "random_careless" — Number of cases up to proportion_biased_cases are sampled and replaced by values from a random uniform distribution ranging between the lowest and highest response category for each variable. These values then replace the values in the original data</li> <li>• "straight_line" — Coming soon...</li> </ul>
proportion_negative	Numeric (length = 1 or factors). Proportion of variables that should have negative (or flipped) dominant loadings across all or each factor. Accepts number of variables as well. The first variables on each factor, up to the corresponding



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**References**

Garcia-Pardina, A., Abad, F. J., Christensen, A. P., Golino, H., & Garrido, L. E. (2022). Dimensionality assessment in the presence of wording effects: A network psychometric and factorial approach. *PsyArXiv*.

Garrido, L. E., Golino, H., Christensen, A. P., Martinez-Molina, A., Arias, V. B., Guerra-Pena, K., ... & Abad, F. J. (2022). A systematic evaluation of wording effects modeling under the exploratory structural equation modeling framework. *PsyArXiv*.

**Examples**

```
# Generate factor data
two_factor <- simulate_factors(
  factors = 2, # factors = 2
  variables = 6, # variables per factor = 6
  loadings = 0.55, # loadings between = 0.45 to 0.65
  cross_loadings = 0.05, # cross-loadings N(0, 0.05)
  correlations = 0.30, # correlation between factors = 0.30
  sample_size = 1000, # number of cases = 1000
  variable_categories = 5 # 5-point Likert scale
)

# Add wording effects using acquiescence method
two_factor_acquiescence <- add_wording_effects(
  lf_object = two_factor,
  proportion_negative = 0.50,
  proportion_biased_cases = 0.10,
  method = "acquiescence"
)

# Add wording effects using difficulty method
two_factor_difficulty <- add_wording_effects(
  lf_object = two_factor,
  proportion_negative = 0.50,
  proportion_biased_cases = 0.10,
  method = "difficulty"
)

# Add wording effects using random careless method
two_factor_random_careless <- add_wording_effects(
  lf_object = two_factor,
  proportion_negative = 0.50,
  proportion_biased_cases = 0.10,
  method = "random_careless"
)

# Add wording effects using straight line method
two_factor_random_careless <- add_wording_effects(
```

```
lf_object = two_factor,
proportion_negative = 0.50,
proportion_biased_cases = 0.10,
method = "straight_line"
)

# Add wording effects using mixed method
two_factor_mixed <- add_wording_effects(
  lf_object = two_factor,
  proportion_negative = 0.50,
  proportion_biased_cases = 0.10,
  method = "mixed"
)

# Add wording effects using acquiescence and straight line method
two_factor_multiple <- add_wording_effects(
  lf_object = two_factor,
  proportion_negative = 0.50,
  proportion_biased_cases = 0.10,
  method = c("acquiescence", "straight_line")
)
```

---

categorize

*Categorize Continuous Data*

---

### Description

Categorizes continuous data based on Garrido, Abad and Ponsoda (2011; see references). Categorical data with 2 to 6 categories can include skew between -2 to 2 in increments of 0.05

### Usage

```
categorize(data, categories, skew_value = 0)
```

### Arguments

data	Numeric (length = n). A vector of continuous data with $n$ values. For matrices, use <code>apply</code>
categories	Numeric (length = 1). Number of categories to create. Between 2 and 6 categories can be used with skew
skew_value	Numeric (length = 1). Value of skew. Ranges between -2 to 2 in increments of 0.05. Skews not in this sequence will be converted to the nearest value in this sequence. Defaults to 0 or no skew

### Value

Returns a numeric vector of the categorize data

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**References**

- Garrido, L. E., Abad, F. J., & Ponsoda, V. (2011). Performance of Velicer's minimum average partial factor retention method with categorical variables. *Educational and Psychological Measurement, 71*(3), 551-570.
- Golino, H., Shi, D., Christensen, A. P., Garrido, L. E., Nieto, M. D., Sadana, R., ... & Martinez-Molina, A. (2020). Investigating the performance of exploratory graph analysis and traditional techniques to identify the number of latent factors: A simulation and tutorial. *Psychological Methods, 25*(3), 292-320.

**Examples**

```
# Dichotomous data (no skew)
dichotomous <- categorize(
  data = rnorm(1000),
  categories = 2
)

# Dichotomous data (with positive skew)
dichotomous_skew <- categorize(
  data = rnorm(1000),
  categories = 2,
  skew_value = 1.25
)

# 5-point Likert scale (no skew)
five_likert <- categorize(
  data = rnorm(1000),
  categories = 5
)

# 5-point Likert scale (negative skew)
five_likert <- categorize(
  data = rnorm(1000),
  categories = 5,
  skew_value = -0.45
)
```



**Description**

Zipf's distribution is commonly found for text data. Closely related to the Pareto and power-law distributions, the Zipf's distribution produces highly skewed data. This transformation is intended to mirror the data generating process of Zipf's law seen in semantic network and topic modeling data.

**Usage**

```
data_to_zipfs(lf_object, beta = 2.7, alpha = 1, dichotomous = FALSE)
```

**Arguments**

lf_object	Data object from <a href="#">simulate_factors</a>
beta	Numeric (length = 1). Sets the shift in rank. Defaults to 2.7
alpha	Numeric (length = 1). Sets the power of the rank. Defaults to 1
dichotomous	Boolean (length = 1). Whether data should be dichotomized rather than frequencies (e.g., semantic network analysis). Defaults to FALSE

**Details**

The formula used to transform data is (Piantadosi, 2014):

$f(r)$  proportional to  $1 / (r + \text{beta})^\alpha$

where  $f(r)$  is the  $r$ th most frequency,  $r$  is the rank-order of the data,  $\text{beta}$  is a shift in the rank (following Mandelbrot, 1953, 1962), and  $\alpha$  is the power of the rank with greater values suggesting greater differences between the largest frequency to the next, and so forth.

The function will transform continuous data output from [simulate\\_factors](#). See examples to get started

**Value**

Returns a list containing:

data	Simulated data that has been transform to follow Zipf's distribution
RMSE	A vector of root mean square errors for transformed data and data assumed to follow theoretical Zipf's distribution and Spearman's correlation matrix of the transformed data compared to the original population correlation matrix
spearman_correlation	Spearman's correlation matrix of the transformed data
original_correlation	Original population correlation matrix <i>before</i> the data were transformed
original_results	Original lf_object input into function

**Author(s)**

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## References

- Mandelbrot, B. (1953). An informational theory of the statistical structure of language. *Communication Theory*, 84, 486–502.
- Mandelbrot, B. (1962). On the theory of word frequencies and on related Markovian models of discourse. *Structure of Language and its Mathematical Aspects*, 190–219.
- Piantadosi, S. T. (2014). Zipf's word frequency law in natural language: A critical review and future directions. *Psychonomic Bulletin & Review*, 21(5), 1112-1130.
- Zipf, G. (1936). *The psychobiology of language*. London, UK: Routledge.
- Zipf, G. (1949). *Human behavior and the principle of least effort*. New York, NY: Addison-Wesley.

## Examples

```
# Generate factor data
two_factor <- simulate_factors(
  factors = 2, # factors = 2
  variables = 6, # variables per factor = 6
  loadings = 0.55, # loadings between = 0.45 to 0.65
  cross_loadings = 0.05, # cross-loadings N(0, 0.05)
  correlations = 0.30, # correlation between factors = 0.30
  sample_size = 1000 # number of cases = 1000
)

# Transform data to Mandelbrot's Zipf's
two_factor_zipfs <- data_to_zipfs(
  lf_object = two_factor,
  beta = 2.7,
  alpha = 1
)

# Transform data to Mandelbrot's Zipf's (dichotomous)
two_factor_zipfs_binary <- data_to_zipfs(
  lf_object = two_factor,
  beta = 2.7,
  alpha = 1,
  dichotomous = TRUE
)
```

## Description

Estimates the number of dimensions in data using Empirical Kaiser Criterion (Braeken & Van Assen, 2017). See examples to get started

**Usage**

```
EKC(data, sample_size)
```

**Arguments**

data	Matrix or data frame. Either a dataset with all numeric values (rows = cases, columns = variables) or a symmetric correlation matrix
sample_size	Numeric (length = 1). If input into data is a correlation matrix, then specifying the sample size is required

**Value**

Returns a list containing:

dimensions	Number of dimensions identified
eigenvalues	Eigenvalues
reference	Reference values compared against eigenvalues

**Author(s)**

Alexander P. Christensen <alexpaulchristensen@gmail.com>, Hudson Golino <hfg9s@virginia.edu>, Luis Eduardo Garrido <luisgarrido@pucmm.edu>

**References**

Braeken, J., & Van Assen, M. A. (2017). An empirical Kaiser criterion. *Psychological Methods*, 22(3), 450–466.

**Examples**

```
# Generate factor data
two_factor <- simulate_factors(
  factors = 2, # factors = 2
  variables = 6, # variables per factor = 6
  loadings = 0.55, # loadings between = 0.45 to 0.65
  cross_loadings = 0.05, # cross-loadings N(0, 0.05)
  correlations = 0.30, # correlation between factors = 0.30
  sample_size = 1000 # number of cases = 1000
)

# Perform Empirical Kaiser Criterion
EKC(two_factor$data)
```

ESEM

*Estimates Exploratory Structural Equation Model***Description**

A general function to estimate an Exploratory Structural Equation Model (ESEM) using the [lavaan](#) package. With [latentFactor](#) objects, the function requires fewer inputs

**Usage**

```
ESEM(
  data,
  factors,
  variables,
  estimator = c("MLR", "WLSMV"),
  fit_measures = NULL,
  variable_polarity = NULL,
  wording_factor = c("none", "CTCM1", "CTCM1_each", "RI", "RI_each"),
  CTCM1_polarity = c("negative", "positive"),
  ...
)
```

**Arguments**

<code>data</code>	Numeric matrix, data frame, or <a href="#">latentFactor</a> object
<code>factors</code>	Numeric (length = 1). Number of ESEM factors to estimate
<code>variables</code>	Numeric (length = 1 or factors). Number of variables per factor. A vector the length of the number of factors can be specified to allow varying number of variables on each factor (necessary for some <code>wording_factor</code> arguments)
<code>estimator</code>	Character. Estimator to be used in <a href="#">cfa</a> . Default options are "MLR" for continuous data and "WLSMV" for categorical data
<code>fit_measures</code>	Character. Fit measures to be computed using <a href="#">fitMeasures</a> . Defaults to: "chisq", "df", "pvalue", "cfi", "tli", "rmsea", "rmsea.ci.lower", "rmsea.ci.upper", "rmsea.pvalue", and "srmr". Other measures can be added but these measures will always be produced. If scaled values are available (not NA), then scaled fit measures will be used.
<code>variable_polarity</code>	Numeric/character (length = 1 or total variables). Whether all (length = 1) or each variable (length = total variables) are positive (1, "p", "pos", "positive") or negative (-1, "n", "neg", "negative") polarity on the factor
<code>wording_factor</code>	Character (length = 1). Whether wording factor(s) should be estimated. Defaults to "none". Options include: <ul style="list-style-type: none"> <li>"CTCM1" — Description coming soon...</li> <li>"CTCM1_each" — Description coming soon...</li> </ul>

- "RI" — Description coming soon...
- "RI\_each" — Description coming soon...

CTCM1\_polarity Character. Polarity of the CTCM1 wording factor(s). Defaults to "negative" for negative polarity variables

... Additional arguments to be passed on to `cfa`

### Value

Returns a list containing:

<code>model</code>	Estimated ESEM model
<code>fit</code>	Fit measures of estimated ESEM model

### Author(s)

Alexander P. Christensen <alexpaulchristensen@gmail.com>, Luis Eduardo Garrido <luisgarrido@pucmm.edu>

### Examples

```
# Generate factor data
two_factor <- simulate_factors(
  factors = 2, # factors = 2
  variables = 6, # variables per factor = 6
  loadings = 0.55, # loadings between = 0.45 to 0.65
  cross_loadings = 0.05, # cross-loadings N(0, 0.05)
  correlations = 0.30, # correlation between factors = 0.30
  sample_size = 1000, # number of cases = 1000
  variable_categories = 5 # 5-point Likert scale
)

## Not run:
# Estimate ESEM model with no wording effects
esem_no_wording_effects <- ESEM(
  data = two_factor,
  estimator = "WLSMV"
)

# Add wording effects using acquiescence method
two_factor_acquiescence <- add_wording_effects(
  lf_object = two_factor,
  proportion_negative = 0.50,
  proportion_biased_cases = 0.10,
  method = "acquiescence"
)

# Estimate ESEM model with wording effects
esem_wording_effects <- ESEM(
  data = two_factor_acquiescence,
  estimator = "WLSMV",
  wording_factor = "RI"
)
```

```
## End(Not run)
```

---

```
estimate_dimensions Estimates Dimensions using Several State-of-the-art Methods
```

---

## Description

Estimates dimensions using Exploratory Graph Analysis ([EGA](#)), Empirical Kaiser Criterion ([EKC](#)), Factor Forest ([factor\\_forest](#)), Exploratory Factor Analysis with out-of-sample prediction ([fspe](#)), Next Eigenvalue Sufficiency Test ([NEST](#)), and parallel analysis ([fa.parallel](#))

## Usage

```
estimate_dimensions(
  data,
  sample_size,
  EGA_args = list(corr = "auto", uni.method = "louvain", model = "glasso",
    consensus.method = "most_common", plot.EGA = FALSE),
  FF_args = list(maximum_factors = 8, PA_correlation = "cor"),
  FSPE_args = list(maxK = 8, rep = 1, method = "PE", pbar = FALSE),
  NEST_args = list(iterations = 1000, maximum_iterations = 500, alpha = 0.05, convergence
    = 0.00001),
  PA_args = list(fm = "minres", fa = "both", cor = "cor", n.iter = 20, sim = FALSE, plot
    = FALSE)
)
```

## Arguments

<code>data</code>	Matrix or data frame. Either a dataset with all numeric values (rows = cases, columns = variables) or a symmetric correlation matrix
<code>sample_size</code>	Numeric (length = 1). If input into data is a correlation matrix, then specifying the sample size is required
<code>EGA_args</code>	List. List of arguments to be passed along to <a href="#">EGA</a> . Defaults are listed
<code>FF_args</code>	List. List of arguments to be passed along to <a href="#">factor_forest</a> . Defaults are listed
<code>FSPE_args</code>	List. List of arguments to be passed along to <a href="#">fspe</a> . Defaults are listed
<code>NEST_args</code>	List. List of arguments to be passed along to <a href="#">NEST</a> . Defaults are listed
<code>PA_args</code>	List. List of arguments to be passed along to <a href="#">fa.parallel</a> . Defaults are listed

## Value

Returns a list containing:

`dimensions`      Dimensions estimated from each method

A list of each methods output (see their respective functions for their outputs)

**Author(s)**

Maria Dolores Nieto Canaveras <mnietoca@nebrija.es>, Alexander P. Christensen <alexpaulchristensen@gmail.com>, Hudson Golino <hfg9s@virginia.edu>, Luis Eduardo Garrido <luisgarrido@pucmm.edu>

**Examples**

```
# Generate factor data
two_factor <- simulate_factors(
  factors = 2, # factors = 2
  variables = 6, # variables per factor = 6
  loadings = 0.55, # loadings between = 0.45 to 0.65
  cross_loadings = 0.05, # cross-loadings N(0, 0.05)
  correlations = 0.30, # correlation between factors = 0.30
  sample_size = 1000 # number of cases = 1000
)

## Not run:
# Estimate dimensions
estimate_dimensions(two_factor$data)
## End(Not run)
```

---

factor\_forest

*Estimate Number of Dimensions using Factor Forest*

---

**Description**

Estimates the number of dimensions in data using the pre-trained Random Forest model from Goretzko and Buhner (2020, 2022). See examples to get started

**Usage**

```
factor_forest(
  data,
  sample_size,
  maximum_factors = 8,
  PA_correlation = c("cor", "poly", "tet")
)
```

**Arguments**

data	Matrix or data frame. Either a dataset with all numeric values (rows = cases, columns = variables) or a symmetric correlation matrix
sample_size	Numeric (length = 1). If input into data is a correlation matrix, then specifying the sample size is required
maximum_factors	Numeric (length = 1). Maximum number of factors to search over. Defaults to 8

PA\_correlation Character (length = 1). Type of correlation used in `fa.parallel`. Must be set:

- "cor" — Pearson's correlation
- "poly" — Polychoric correlation
- "tet" — Tetrachoric correlation

### Value

Returns a list containing:

dimensions      Number of dimensions identified  
 probabilities    Probability that the number of dimensions is most likely

### Author(s)

# Authors of Factor Forest

David Goretzko and Markus Buhner

# Authors of {latentFactor}

Alexander P. Christensen <alexpaulchristensen@gmail.com>, Hudson Golino <hfg9s@virginia.edu>,  
 Luis Eduardo Garrido <luisgarrido@pucmm.edu>

### References

Goretzko, D., & Buhner, M. (2022). Factor retention using machine learning with ordinal data. *Applied Psychological Measurement*, 01466216221089345.

Goretzko, D., & Buhner, M. (2020). One model to rule them all? Using machine learning algorithms to determine the number of factors in exploratory factor analysis. *Psychological Methods*, 25(6), 776-786.

### Examples

```
# Generate factor data
two_factor <- simulate_factors(
  factors = 2, # factors = 2
  variables = 6, # variables per factor = 6
  loadings = 0.55, # loadings between = 0.45 to 0.65
  cross_loadings = 0.05, # cross-loadings N(0, 0.05)
  correlations = 0.30, # correlation between factors = 0.30
  sample_size = 1000 # number of cases = 1000
)

## Not run:
# Perform Factor Forest
factor_forest(two_factor$data)
## End(Not run)
```



---

NEST *Estimate Number of Dimensions using Next Eigenvalue Sufficiency Test*

---

### Description

Estimates the number of dimensions in data using NEST (Achim, 2017). See examples to get started

### Usage

```
NEST(
  data,
  sample_size,
  iterations = 1000,
  maximum_iterations = 500,
  alpha = 0.05,
  convergence = 0.00001
)
```

### Arguments

data	Matrix or data frame. Either a dataset with all numeric values (rows = cases, columns = variables) or a symmetric correlation matrix
sample_size	Numeric (length = 1). If input into data is a correlation matrix, then specifying the sample size is required
iterations	Numeric (length = 1). Number of iterations to estimate rank. Defaults to 1000
maximum_iterations	Numeric (length = 1). Maximum number of iterations to obtain convergence of eigenvalues. Defaults to 500
alpha	Numeric (length = 1). Significance level for determine sufficient eigenvalues. Defaults to 0.05
convergence	Numeric (length = 1). Value necessary to be less than or equal to when establishing convergence of eigenvalues

### Value

Returns a list containing:

dimensions	Number of dimensions identified
loadings	Loading matrix
converged	Whether estimation converged. If FALSE, then results are reported from last convergence point. Interpret results with caution.

### Author(s)

Alexander P. Christensen <alexpaulchristensen@gmail.com>, Hudson Golino <hfg9s@virginia.edu>, Luis Eduardo Garrido <luisgarrido@pucmm.edu>

## References

Achim, A. (2017). Testing the number of required dimensions in exploratory factor analysis. *The Quantitative Methods for Psychology*, 13(1), 64–74.

Brandenburg, N., & Papenberg, M. (2022). Reassessment of innovative methods to determine the number of factors: A simulation-Based comparison of Exploratory Graph Analysis and Next Eigenvalue Sufficiency Test. *Psychological Methods*.

## Examples

```
# Generate factor data
two_factor <- simulate_factors(
  factors = 2, # factors = 2
  variables = 6, # variables per factor = 6
  loadings = 0.55, # loadings between = 0.45 to 0.65
  cross_loadings = 0.05, # cross-loadings N(0, 0.05)
  correlations = 0.30, # correlation between factors = 0.30
  sample_size = 1000 # number of cases = 1000
)

## Not run:
# Perform NEST
NEST(two_factor$data)
## End(Not run)
```

---

```
obtain_zipfs_parameters
```

*Obtain Zipf's Distribution Parameters from Data*

---

## Description

Zipf's distribution is commonly found for text data. Closely related to the Pareto and power-law distributions, the Zipf's distribution produces highly skewed data. This function obtains the best fitting parameters to Zipf's distribution

## Usage

```
obtain_zipfs_parameters(data)
```

## Arguments

data	Numeric vector, matrix, or data frame. Numeric data to determine Zipf's distribution parameters
------	---

**Details**

The best parameters are optimized by minimizing the absolute difference between the original frequencies and the frequencies obtained by the *beta* and *alpha* parameters in the following formula (Piantadosi, 2014):

$$f(r) \text{ proportional to } 1 / (r + \textit{beta})^{\textit{alpha}}$$

where  $f(r)$  is the  $r$ th most frequency,  $r$  is the rank-order of the data, *beta* is a shift in the rank (following Mandelbrot, 1953, 1962), and *alpha* is the power of the rank with greater values suggesting greater differences between the largest frequency to the next, and so forth.

**Value**

Returns a vector containing the estimated beta and alpha parameters. Also contains zipfs\_sse which corresponds to the sum of square error between frequencies based on the parameter values estimated and the original data frequencies

**Author(s)**

Alexander P. Christensen <alexpaulchristensen@gmail.com>, Hudson Golino <hfg9s@virginia.edu>, Luis Eduardo Garrido <luisgarrido@pucmm.edu>

**References**

- Mandelbrot, B. (1953). An informational theory of the statistical structure of language. *Communication Theory*, 84, 486–502.
- Mandelbrot, B. (1962). On the theory of word frequencies and on related Markovian models of discourse. *Structure of Language and its Mathematical Aspects*, 190–219.
- Piantadosi, S. T. (2014). Zipf's word frequency law in natural language: A critical review and future directions. *Psychonomic Bulletin & Review*, 21(5), 1112-1130.

**Examples**

```
# Generate factor data
two_factor <- simulate_factors(
  factors = 2, # factors = 2
  variables = 6, # variables per factor = 6
  loadings = 0.55, # loadings between = 0.45 to 0.65
  cross_loadings = 0.05, # cross-loadings N(0, 0.05)
  correlations = 0.30, # correlation between factors = 0.30
  sample_size = 1000 # number of cases = 1000
)

# Transform data to Mandelbrot's Zipf's
two_factor_zipfs <- data_to_zipfs(
  lf_object = two_factor,
  beta = 2.7,
  alpha = 1
)

# Obtain Zipf's distribution parameters
```

```
obtain_zipfs_parameters(two_factor_zipfs$data)
```

---

simulate\_factors      *Simulates Latent Factor Data*

---

## Description

Simulates data from a latent factor model based on many manipulable parameters. Parameters do not have default values and must each be set. See examples to get started

## Usage

```
simulate_factors(
  factors,
  variables,
  variables_range = NULL,
  loadings,
  loadings_range = NULL,
  cross_loadings,
  cross_loadings_range = NULL,
  correlations,
  correlations_range = NULL,
  sample_size,
  variable_categories = Inf,
  categorical_limit = 7,
  skew = 0,
  skew_range = NULL
)
```

## Arguments

factors	Numeric (length = 1). Number of factors
variables	Numeric (length = 1 or factors). Number of variables per factor. Can be a single value or as many values as there are factors. Minimum three variables per factor
variables_range	Numeric (length = 2). Range of variables to randomly select from a random uniform distribution. Minimum three variables per factor
loadings	Numeric or matrix (length = 1, factors, total number of variables (factors x variables), or factors x total number of variables). Loadings drawn from a random uniform distribution using +/- 0.10 of value input. Can be a single value or as many values as there are factors (corresponding to the factors). Can also be a loading matrix. Columns must match factors and rows must match total variables (factors x variables) General effect sizes range from small (0.40), moderate (0.55), to large (0.70)

loadings_range	Numeric (length = 2). Range of loadings to randomly select from a random uniform distribution. General effect sizes range from small (0.40), moderate (0.55), to large (0.70)
cross_loadings	Numeric or matrix(length = 1, factors, or factors x total number of variables). Cross-loadings drawn from a random normal distribution with a mean of 0 and standard deviation of value input. Can be a single value or as many values as there are factors (corresponding to the factors). Can also be a loading matrix. Columns must match factors and rows must match total variables (factors x variables)
cross_loadings_range	Numeric (length = 2). Range of cross-loadings to randomly select from a random uniform distribution
correlations	Numeric (length = 1 or factors x factors). Can be a single value that will be used for all correlations between factors. Can also be a square matrix (factors x factors). General effect sizes range from orthogonal (0.00), small (0.30), moderate (0.50), to large (0.70)
correlations_range	Numeric (length = 2). Range of correlations to randomly select from a random uniform distribution. General effect sizes range from orthogonal (0.00), small (0.30), moderate (0.50), to large (0.70)
sample_size	Numeric (length = 1). Number of cases to generate from a random multivariate normal distribution using <code>rmvnorm</code>
variable_categories	Numeric (length = 1 or total variables (factors x variables)). Number of categories for each variable. Inf is used for continuous variables; otherwise, values reflect number of categories
categorical_limit	Numeric (length = 1). Values greater than input value are considered continuous. Defaults to 7 meaning that 8 or more categories are considered continuous (i.e., variables are <i>not</i> categorized from continuous to categorical)
skew	Numeric (length = 1 or categorical variables). Skew to be included in categorical variables. It is randomly sampled from provided values. Can be a single value or as many values as there are (total) variables. Current skew implementation is between -2 and 2 in increments of 0.05. Skews that are not in this sequence will be converted to their nearest value in the sequence. Not recommended to use with <code>variables_range</code> . Future versions will incorporate finer skews
skew_range	Numeric (length = 2). Randomly selects skews within in the range. Somewhat redundant with <code>skew</code> but more flexible. Compatible with <code>variables_range</code>

## Value

Returns a list containing:

data	Simulated data from the specified factor model
population_correlation	Population correlation matrix

parameters      A list containing the parameters used to generate the data:

- factors — Number of factors
- variables — Variables on each factor
- loadings — Loading matrix
- factor\_correlations — Correlations between factors
- categories — Categories for each variable
- skew — Skew for each variable

### Author(s)

Maria Dolores Nieto Canaveras <mnietoca@nebrija.es>, Alexander P. Christensen <alexpaulchristensen@gmail.com>, Hudson Golino <hfg9s@virginia.edu>, Luis Eduardo Garrido <luisgarrido@pucmm.edu>

### References

Garrido, L. E., Abad, F. J., & Ponsoda, V. (2011). Performance of Velicer's minimum average partial factor retention method with categorical variables. *Educational and Psychological Measurement*, 71(3), 551-570.

Golino, H., Shi, D., Christensen, A. P., Garrido, L. E., Nieto, M. D., Sadana, R., ... & Martinez-Molina, A. (2020). Investigating the performance of exploratory graph analysis and traditional techniques to identify the number of latent factors: A simulation and tutorial. *Psychological Methods*, 25(3), 292-320.

### Examples

```
# Generate factor data
two_factor <- simulate_factors(
  factors = 2, # factors = 2
  variables = 6, # variables per factor = 6
  loadings = 0.55, # loadings between = 0.45 to 0.65
  cross_loadings = 0.05, # cross-loadings N(0, 0.05)
  correlations = 0.30, # correlation between factors = 0.30
  sample_size = 1000 # number of cases = 1000
)

# Randomly vary loadings
two_factor_loadings <- simulate_factors(
  factors = 2, # factors = 2
  variables = 6, # variables per factor = 6
  loadings_range = c(0.30, 0.80), # loadings between = 0.30 to 0.80
  cross_loadings = 0.05, # cross-loadings N(0, 0.05)
  correlations = 0.30, # correlation between factors = 0.30
  sample_size = 1000 # number of cases = 1000
)

# Generate dichotomous data
two_factor_dichotomous <- simulate_factors(
  factors = 2, # factors = 2
  variables = 6, # variables per factor = 6
```

```

loadings = 0.55, # loadings between = 0.45 to 0.65
cross_loadings = 0.05, # cross-loadings N(0, 0.05)
correlations = 0.30, # correlation between factors = 0.30
sample_size = 1000, # number of cases = 1000
variable_categories = 2 # dichotomous data
)

# Generate dichotomous data with skew
two_factor_dichotomous_skew <- simulate_factors(
  factors = 2, # factors = 2
  variables = 6, # variables per factor = 6
  loadings = 0.55, # loadings between = 0.45 to 0.65
  cross_loadings = 0.05, # cross-loadings N(0, 0.05)
  correlations = 0.30, # correlation between factors = 0.30
  sample_size = 1000, # number of cases = 1000
  variable_categories = 2, # dichotomous data
  skew = 1 # all variables with have a skew of 1
)

# Generate dichotomous data with variable skew
two_factor_dichotomous_skew <- simulate_factors(
  factors = 2, # factors = 2
  variables = 6, # variables per factor = 6
  loadings = 0.55, # loadings between = 0.45 to 0.65
  cross_loadings = 0.05, # cross-loadings N(0, 0.05)
  correlations = 0.30, # correlation between factors = 0.30
  sample_size = 1000, # number of cases = 1000
  variable_categories = 2, # dichotomous data
  skew_range = c(-2, 2) # skew = -2 to 2 (increments of 0.05)
)

```

---

skew\_tables

*Skew Tables*


---

### Description

Tables for skew based on the number of categories (2, 3, 4, 5, or 6) in the data

### Usage

```
data(skew_tables)
```

### Format

A list (length = 5)

### Examples

```
data("skew_tables")
```

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